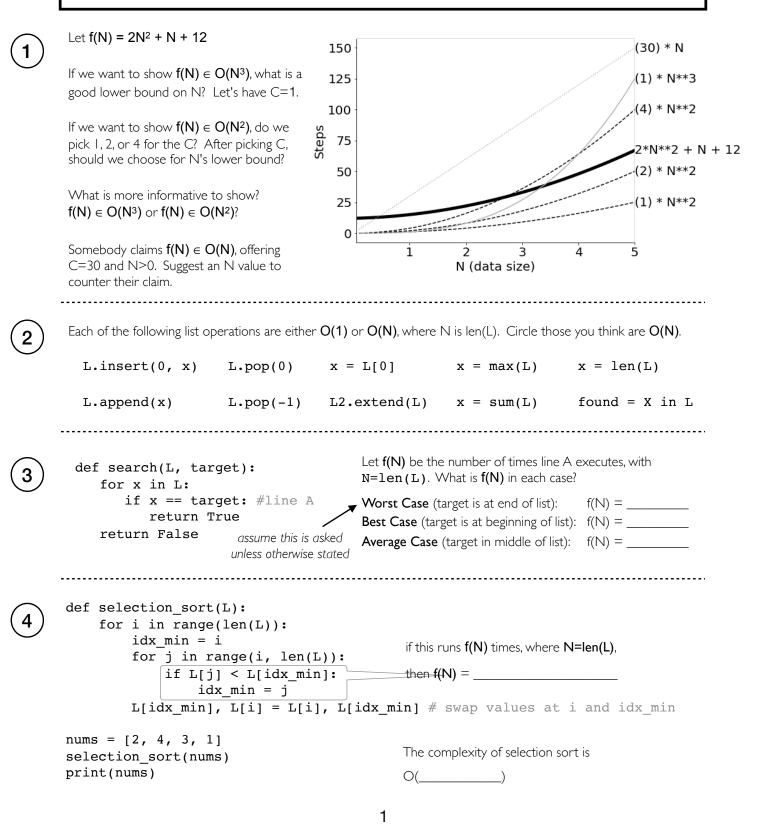
## Lecture 5 Worksheet: Complexity Analysis

A step is any unit of work with bounded execution time (it doesn't keep getting slower with growing input size).

We classify algorithm complexity by classifying the **order of growth** of a function f(N), where f gives the number of steps the algorithm must perform for a given input size.

Big O definition: if  $f(N) \le C * g(N)$  for large N values and some fixed constant C, then  $f(N) \in O(g(N))$ 



```
# assume L is already sorted, N=len(L)
5
     def binary search(L, target):
                                                              how many times does this step run
          left idx = 0 # inclusive
                                                              when N = 1? N = 2? N = 4? N = 8?
          right_idx = len(L) # exclusive
          while right idx - left idx > 1:
                                                              If f(N) is the number of times this step
              mid_idx = (right_idx + left_idx) // 2
                                                              runs, then f(N) = _
              mid = L[mid idx]
              if target >= mid:
                                                              The complexity of binary search is
                   left_idx = mid_idx
                                                              O(_____)
              else:
                  right_idx = mid_idx
          return right_idx > left_idx and L[left_idx] == target
                                                          def merge sort(L):
      def merge(L1, L2):
6
        rv = []
                                                            if len(L) < 2:
        idx1 = 0
                                                              return L
                                                            mid = len(L) // 2
        idx2 = 0
                                                            left = L[:mid]
        while True:
                                                            right = L[mid:]
          done1 = idx1 == len(L1)
                                                            left = merge sort(left)
          done2 = idx2 == len(L2)
                                                            right = merge sort(right)
                                                            return merge(left, right)
          if done1 and done2:
                                                          merge_sort([4, 1, 2, 3])
             return rv
          choose1 = False
                                                                                7 8
                                                              1
                                                                 2
                                                                    3
                                                                       4
                                                                          5
                                                                             6
          if done2:
                                                                         ♣
             choose1 = True
                                                                       MS
          elif not done1 and L1[idx1] < L2[idx2]:
             choose1 = True
                                                             2
                                                                3
                                                                   7
                                                                      8
                                                                           1
                                                                              4
                                                                                 5
                                                                                    6
          if choosel:
                                                                  ▲
                                                                                ۸
                                                                MS
                                                                               MS
             rv.append(L1[idx1])
             idx1 += 1
                                                                   2
                                                                8
                                                                       3
                                                                           4
                                                                              5
                                                                                     6
                                                            7
                                                                                  1
          else:
             rv.append(L2[idx2])
                                                                           MS
                                                             MS
                                                                    MS
                                                                                  MS
             idx2 += 1
```

merge([1, 3], [2, 4]) will return \_\_\_\_\_\_ merge(L1, L2) implements an O(N) algorithm. But how can we measure the size of the input? N = \_\_\_\_\_.

\_\_\_\_\_

If we double the list size, there will be \_\_\_\_ more level(s). Level count grows O(\_\_\_\_\_). Work per level is O(\_\_\_\_\_). merge\_sort complexity: O(\_\_\_\_\_)

3 || 5

nums = [...]

first100sum = 0

return rv

```
for x in nums[:100]:
    first100sum += x
print(first100sum)
```

If we increase the size of nums from 20 items to 100 items, the code will probably take \_\_\_\_\_\_ times longer to run.

If we increase the size of nums from 100 to 1000, will the code take longer? Yes / No  $\,$ 

The complexity of the code is O(\_\_\_\_), with N=len(nums).