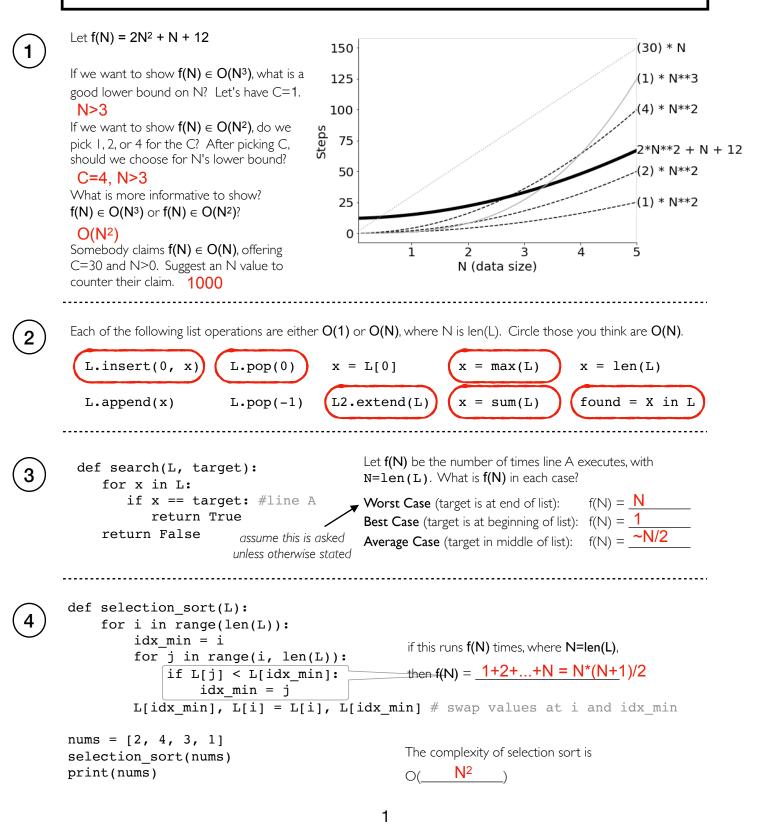
Lecture 5 Worksheet: Complexity Analysis

A step is any unit of work with bounded execution time (it doesn't keep getting slower with growing input size).

We classify algorithm complexity by classifying the **order of growth** of a function f(N), where f gives the number of steps the algorithm must perform for a given input size.

Big O definition: if $f(N) \le C * g(N)$ for large N values and some fixed constant C, then $f(N) \in O(g(N))$



```
left idx = 0 # inclusive
                                                                    when N = 1? N = 2? N = 4? N = 8?
           right_idx = len(L) # exclusive
                                                                                               3
                                                                           0
                                                                                  1
                                                                                        2
           while right idx - left idx > 1:
                                                                    If f(N) is the number of times this step
                mid_idx = (right_idx + left_idx) // 2
                                                                    runs, then f(N) = \log_2(N)
               mid = L[mid idx]
                if target >= mid:
                                                                    The complexity of binary search is
                    left_idx = mid_idx
                                                                    O(\log N)
                                                                                 )
                else:
                    right_idx = mid_idx
           return right_idx > left_idx and L[left_idx] == target
                                                                def merge sort(L):
       def merge(L1, L2):
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         rv = []
                                                                  if len(L) < 2:
         idx1 = 0
                                                                     return L
         idx2 = 0
                                                                  mid = len(L) // 2
                                                                  left = L[:mid]
         while True:
                                                                  right = L[mid:]
            done1 = idx1 == len(L1)
                                                                  left = merge sort(left)
            done2 = idx2 == len(L2)
                                                                  right = merge sort(right)
                                                                  return merge(left, right)
            if done1 and done2:
                                                                merge_sort([4, 1, 2, 3])
              return rv
            choose1 = False
                                                                    1
                                                                       2
                                                                           3
                                                                              4
                                                                                 5
                                                                                     6
                                                                                        7
                                                                                           8
            if done2:
              choose1 = True
                                                                               MS
            elif not done1 and L1[idx1] < L2[idx2]:
              choose1 = True
                                                                   2
                                                                      3
                                                                          7
                                                                             8
                                                                                   1
                                                                                      4
                                                                                         5
                                                                                             6
            if choosel:
                                                                        ▲
                                                                                        ۸
                                                                       MS
                                                                                       MS
              rv.append(L1[idx1])
              idx1 += 1
                                                                          2
                                                                      8
                                                                              3
                                                                                     5
                                                                                             6
                                                                   7
                                                                                  4
                                                                                          1
            else:
              rv.append(L2[idx2])
                                                                                   MS
                                                                   MS
                                                                           MS
                                                                                           MS
              idx2 += 1
         return rv
                                                                                  5
                                           [1, 2, 3, 4]
                                                                If we double the list size, there will be ____
      merge([1, 3], [2, 4]) will return _
                                                                more level(s). Level count grows
      merge(L1, L2) implements an O(N) algorithm. But how
                                                                O(100 \text{ N}). Work per level is O(-100 \text{ N})
                                                                                            Ν
       can we measure the size of the input? N = \frac{len(L1)}{L1} + len(L2)
                                                                merge_sort complexity: O(<u>N</u> log N)
      _____
                                          If we increase the size of nums from 20 items to 100 items, the code
      nums = [\ldots]
                                          will probably take <u>b</u> times longer to run.
      first100sum = 0
                                          If we increase the size of nums from 100 to 1000, will the code take
      for x in nums[:100]:
                                          longer? Yes No
           first100sum += x
      print(first100sum)
```

assume L is already sorted, N=len(L)

def binary search(L, target):

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The complexity of the code is O(1), with N=len(nums).

how many times does this step run